

**ARULMIGU PALANIANDAVAR ARTS COLLEGE
FOR WOMEN, PALANI**

DEPARTMENT OF MATHEMATICS

ALLIED MATHEMATICS II :

**INTEGRAL CALCULUS, DIFFERENTIAL EQUATIONS, LAPLACE
TRANSFORMS AND VECTOR ANALYSIS**

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**ARULMIGU PALANIANDAVAR ARTS COLLEGE FOR
WOMEN (AUTONOMOUS)**

(Affiliated to Mother Teresa Women's university)

Palani – 624 615.

Integral calculus, Differential Equations, Laplace Transform and
Vector Analysis.

Allied Mathematics - II

UNIT - I

1. State Bernoulli's Theorem

(Ans: $\int uv dx = uv_1 - u'v_2 + u''v_3 - u'''v_4 + \dots$)

2. If $f(x)$ is an odd function of x , then $\int_{-a}^a f(x) dx = \underline{\hspace{2cm}}$.

(Ans: 0)

3. If $f(x)$ is an even function of x , then $\int_{-a}^a f(x) dx = \underline{\hspace{2cm}}$.

(Ans: $2\int_0^a f(x) dx$)

4. The value of $\int_0^{\frac{\pi}{2}} \sin^4 x dx$ is given by

a) $\frac{3\pi}{16}$ b) $\frac{5\pi}{8}$ c) $\frac{3\pi}{8}$ d) $\frac{3}{8}$

(Ans: a)

5. The value of $\int \tan x dx = \underline{\hspace{2cm}}$.

(Ans: $\log \sec x + c$)

6. $\int f(x) dx$ is called $\underline{\hspace{2cm}}$ the range of integration is not specified

(Ans: Indefinite integral)

7. The value of $\int_0^1 (3x^2 + 2x) dx$ is given by

a) 0 b) 2 c) 1 d) -1

(Ans: b)

8. The value of $\int \sec x dx$ is given by

a) $\log \cos x + c$ b) $\log \sin x + c$ c) $\log \sec x + c$
b) d) $\log (\sec x + \tan x) + c$

(Ans: d)

9. $\underline{\hspace{2cm}}$ is the standard device for integration.

(Ans: Integration by parts)

10. The value of $\int \coth x \, dx =$ _____.
 a) $\log \cosh x + c$ b) $\log \sinh x + c$ c) $\log \tanh x + c$ d) None
 (Ans: b)

11. The value of $\int_0^{\frac{\pi}{2}} \cos^5 x \, dx =$ _____.
 a) $\frac{4}{15}$ b) $\frac{8}{15}$ c) $\frac{15}{8}$ d) $\frac{5}{6}$
 (Ans: b)

12. The value of $\int_0^{\frac{\pi}{2}} \sin^6 x \, dx$ is given by
 a) $\frac{32}{5\pi}$ b) $\frac{5\pi}{32}$ c) $\frac{15}{48}$ d) $\frac{5\pi}{64}$
 (Ans: b)

13. $\int_0^{\frac{\pi}{2}} \sin^n x \, dx =$ ____ if n is even integer.
 (Ans: $\frac{n-1}{n} \cdot \frac{n-3}{n-2} \cdot \frac{n-5}{n-4} \dots \frac{1}{2} \cdot \frac{\pi}{2}$)

14. A formula by which the power of any variable in the integral is reduced is called a _____.
 (Ans: Reduction formula)

15. $f(x)$ is odd if $f(-x) =$ _____
 a) $-f(x)$ b) $2f(x)$ c) 0 d) $-f(-x)$
 (Ans: a)

16. The value of $\int \frac{1}{x} \cdot \frac{1}{\sqrt{1+\log x}} \, dx$ is given by
 a) $\log \sqrt{1+\log x} + c$ b) $e^x(1+\log x) + c$
 c) $2\sqrt{1+\log x} + c$ d) $e^x \sqrt{1+\log x} + c$
 (Ans: c)

17. The value of $\int \frac{e^x}{e^x+20} \, dx =$ _____.
 (Ans: $\log(e^x + 20) + c$)

18. The value of $\int \cos(ax + b) \, dx =$ _____.
 (Ans: $\frac{1}{a} \sin(ax + b) + c$)

19. The value of $\int \frac{1}{ax+b} \, dx =$ _____.

(Ans: $\frac{1}{a} \log(ax + b) + c$)

20. $\int e^{ax} [a f(x) + f'(x)] dx = \underline{\hspace{2cm}}$.

(Ans: $e^{ax} f(x) + c$)

UNIT - II

21. The smallest positive value of $P f(x + p) = f(x)$ is true for every value of x is called of the function.

(Ans: *period*)

22. $\sin nx$ is a period functions of period .

(Ans: $\frac{2\pi}{n}$)

23. $F(x) = \frac{a_0}{2} + \sum_{n=1}^{\infty} (a_n \cos nx + b_n \sin nx)$ then the RHS series of sines and cosines is called of $f(x)$.

(Ans: *fourier series*)

24. In fourier series $f(x)$ is single valued and finite in .

- a) $(0, \pi)$ b) $[0, (\frac{\pi}{2})]$ c) $(0, 2\pi)$ d) $[0, (\frac{\pi}{4})]$

(Ans: *c*)

25. In fourier series $f(x)$ a number of maxima or minima in $(0, 2\pi)$.

- a) *Infinite* b) *finite* c) *equal* d) *unequal*

(Ans: *b*)

26. In $F(x) = \frac{a_0}{2} + \sum_{n=1}^{\infty} (a_n \cos nx + b_n \sin nx)$ a_0, a_n, b_n are called

(Ans: *fourier co – efficient*)

27. A function $f(x)$ is said to be periodic iff .

[Ans: $f(x + p) = f(x)$]

28. The value of $\sin n\pi = \underline{\hspace{2cm}}$.

(Ans: *0*)

29. The value of $\cos n\pi = \underline{\hspace{2cm}}$.

(Ans: $(-1)^n$)

30. $\int_0^{\pi} f(\sin x) dx = \underline{\hspace{2cm}}$.

- a) $2 \int_0^{\frac{\pi}{2}} f(\sin x) dx$ b) $\int_0^{\frac{\pi}{2}} f(\sin x) dx$ c) $2 \int_0^{\frac{\pi}{2}} f(\sin x) dx$

d) $2 \int_0^{\frac{\pi}{2}} f(\cos x) dx$

(Ans: c)

31. If $f(x)$ is continuous at $x = a$ in $(0, 2\pi)$ then the n value of Fourier series at $x=a$ is equal to _____.

- a) a_0 b) a_n c) $f(a)$ d) $f(x)$

(Ans: c)

32. If $f(x)$ is discontinuous at $x=a$ in $(0, 2\pi)$ then the n value of fourier series at $x=a$ is equal to _____.

- a) $\frac{1}{2} f(a+) + f(a-)$ b) $f(a+) + f(a-)$
 c) $\frac{1}{2} f(a-) - f(a+)$ d) $\frac{1}{2} f(a) - f(a)$

(Ans: a)

33. The value of the fourier at $x=0$ or $x=2\pi$ is equal to the value of _____.

[Ans: $\frac{1}{2} f(0+) + f(2\pi - 1)$]

34. If the fourier series $f(x) = x^2$ in $(-\pi, \pi)$. Find the value of a_0

- a) $\frac{3}{2} \pi^2$ b) $\frac{2}{3} \pi^2$ c) $\frac{2}{3} \pi^3$ d) $\frac{3}{2} \pi^3$

(Ans: b)

35. Say True or False

In the Fourier series $f(x) = x$ in $(-\pi, \pi)$ the value of a_0 is zero.

(Ans: True)

36. In Fourier series $F(x) = \frac{a_0}{2} + \sum_{n=1}^{\infty} (a_n \cos nx + b_n \sin nx)$ where

$a_n =$ _____

(Ans: $\frac{1}{\pi} \int_0^{2\pi} f(x) \cos nx dx$)

37. In Fourier series $F(x) = \frac{a_0}{2} + \sum_{n=1}^{\infty} (a_n \cos nx + b_n \sin nx)$ where

$b_n =$ _____ .

(Ans: $\frac{1}{\pi} \int_0^{2\pi} f(x) \sin nx dx$)

38. If $n \neq 0 \int_c^{c+2\pi} \cos^2 nx dx =$ _____ .

- a) $-\pi$ b) π c) 2π d) 0

(Ans: b)

39. If $n \neq 0$ $\int_0^{2\pi} \sin nx dx =$ _____ .
a) π b) 0 c) 2π d) $-\pi$

(Ans: b)

40. Say True or False

If $m \neq 0$ $\int_0^{2\pi} \sin mx \sin nx dx = 0$

(Ans : True)

UNIT - III

41. An equation is of the form $\sum F_i dx_i = 0$ is called _____ in n.

(Ans : Pfaffian differential equation)

42. An equations of the form $Pdx + Qdy + Rdz = 0$ where P, Q, R are functions of x, y, z is called _____

(Ans : Total differential equation)

43. The auxillary equations can be solved by _____

(Ans: Lagrange's Method)

44. $xP + yQ + zR = C$ is the solution of $Pdx + Qdy + Rdz = 0$ when it is exact and _____ of degree $n \neq -1$

(Ans : Homogeneous)

45. Say true or false

A partial differential equation involves in partial derivatives

(Ans : True)

46) Say true or false

If the number of constants to be eliminated is not equal to the number of independent variables

(Ans : False)

47. The claurit's equation is _____

(Ans : $y = px + f(p)$)

48. The Clairaut's form of $p = \log(px - y)$ is given by _____
a) $y = px - e^p$ b) $y = px + e^p$ c) $y = px + \log p$ d) $y = p - \log px$

(Ans: a)

49. In partial differential equation by eliminating arbitrary constants a & b from $z = (x+a)(x+b)$ is _____

a) $z = p/q$ b) $z = p+q$ c) $z = pq$ d) none

(Ans : $z = pq$)

50. The auxiliary equation of the partial differential equation $2p + 3q = 1$ is _____

(Ans : $\frac{dx}{2} = \frac{dy}{3} = \frac{dz}{1}$)

51. The general solution of $p = \log(px - y)$ is _____

(Ans : $y = px - e^p$)

52. $Pp + Qq = R$ is called _____ linear equation

(Ans : Lagrange)

53. Necessary and sufficient conditions for integrability of

$Pdx + Qdy + Rdz =$ _____

(Ans : 0)

54. If $z = (x^2 + a)(y^2 + b)$ where a, b are constants then $\frac{\partial z}{\partial x} =$ _____

(Ans : $2x + y^2$)

55. Say true or false

The order of partial differential equation is the order of highest derivative occurring in it.

(Ans : True)

56. Say true or false

The partial differential equation of all spheres whose centre is $(a, b, 0)$ and whose radius r is $z^2(p^2 + q^2 + 1) = r^2$

(Ans : True)

57. Form the partial differential equation by eliminating the arbitrary functions from $z = f(x^2 + y^2)$

(Ans : $py - qx = 0$)

58. If $z = x^2 + 2f\left[\frac{1}{y} + \log x\right]$ Find $\frac{\partial z}{\partial x}$

(Ans: $2x + 2f' \left[\frac{1}{y} + \log x\right] \left(\frac{1}{x}\right)$)

59. If $z = f(x^2 + y^2)$ find $\frac{\partial z}{\partial y}$

(Ans : $f' (x^2 + y^2) 2y$)

60. $f(x, y, z, a, b) = 0$ is said to be the _____ of the first order differential equation $\phi(x, y, z, p, q) = 0$

(Ans : Complete Solution)

UNIT - IV

61. $F(s) = \int_0^\infty e^{-st} f(t) dt$ is called _____.

(Ans: Laplace transform)

62. The value of $L(e^{at}) = \frac{1}{s-a}$ if $(s-a) > 0$.

a) $\frac{1}{s^2 + a^2}$ b) $\frac{1}{s+a}$ c) $\frac{a}{s^2 - a^2}$ d) $\frac{1}{s-a}$

(Ans: d)

63. Find Laplace transform of t^n

a) $\frac{n!}{s^{n+1}}$ b) $\frac{n!}{s^n}$ c) $\frac{(n+1)!}{s^{n+1}}$ d) $\frac{(n-1)!}{s^n}$

(Ans: a)

64. If $L[f(t)] = F(s)$ then $L[e^{-at} f(t)] = \frac{F(s+a)}{e^{-at}}$.

(Ans: $[F(s + a)]$)

65. The Inverse Laplace Transform of $\frac{s}{s^2 + a^2}$

a) $\sin at$ b) $\cos at$ c) $\sin ht$ d) $\cos^{-1} at$

(Ans: b)

66. Say True or False

$$L^{-1}[F(s + a)] = e^{-at} L^{-1}[F(s)]$$

(Ans: True)

67. Laplace transform is linear.

(Ans: True)

68. Inverse Laplace transform is linear.

(Ans: True)

69. $L[\sin at \sin bt] = L[\sin at] \cdot L[\sin bt]$

(Ans: false)

70. Laplace transform of $t [f(t)] = \underline{\hspace{2cm}}$.

- a) $\frac{d}{ds} [F(s)]$ b) $-\frac{d}{ds} [F(s)]$ c) $-\frac{d^n}{ds^n} [F(s)]$ d) $\frac{d^n}{ds^n} [F(s)]$

(Ans: b)

71. Laplace transform of $f'(t) = \underline{\hspace{2cm}}$.

(Ans: $sL[f(t)] - f(0)$)

72. Laplace transform of $f''(t) = \underline{\hspace{2cm}}$.

(Ans: $sL[f'(t)] - f'(0)$)

73. $L^{-1} \left[\frac{1}{(s-1)^2} \right]$ is $\underline{\hspace{2cm}}$.

- a) e^t b) $t + e^t$ c) te^{-t} d) te^t

(Ans: d)

74. The Laplace transform L of $f(x)$ is defined by

(Ans: $\int_0^{\infty} e^{-sx} f(x) dx$)

75. The value of $L(1)$ is given by $\underline{\hspace{2cm}}$.

- a) 1 b) 0 c) $\frac{1}{s}$ d) $\frac{1}{2s^{3/2}}$

(Ans : c)

76. $L(\sqrt{x}) = \underline{\hspace{2cm}}$.

- a) $\frac{1}{s^2}$ b) $\frac{\sqrt{\pi}}{2s^{3/2}}$ c) $\frac{\sqrt{\pi}}{3s^{3/2}}$ d) $\frac{\pi}{2s^{3/2}}$

(Ans: b)

77. $L[f(ax)]$ is

- a) $\frac{1}{a} F(s)$ b) $\frac{1}{a} F\left(\frac{s}{a}\right)$ c) $\frac{1}{a} F\left(\frac{a}{s}\right)$ d) $a F(s)$

(Ans: b)

78. Say True or False

If $L[f(t)] = F(s)$, then $L[e^{-at} f(t)] = F(s+a)$ is known as first shifting theorem.

(Ans: True)

79. $L^{-1} \left[\frac{1}{s^n} \right] = \underline{\hspace{2cm}}$.

(Ans: $\frac{t^{n-1}}{(n-1)!}$)

80. $L^{-1}[e^{ax}] = \underline{\hspace{2cm}}$.

(Ans: $\frac{1}{s-a}$)

UNIT - V

81.If $f(p)$ is a vector then the function $f(p)$ is called a _____ function.

(Ans : vector point)

82. $\frac{d}{dt}(r \cdot r) =$ _____

a) $r \frac{dr}{dt}$ b) $2r \frac{dr}{dt}$ c) $r \frac{dt}{dr}$ d) $2r \frac{dt}{dr}$

(Ans : b)

83.If f is a constant vector $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$ are all zeros and hence _____

(Ans : curl $f=0$ or div $f=0$)

84.If f is a vector such that curl $f=0$ for all points in the region ,then it is called an _____

(Ans : irrotational vector)

85.Grad ϕ is defined by _____

(Ans : $\nabla\phi = i \frac{\partial\phi}{\partial x} + j \frac{\partial\phi}{\partial y} + k \frac{\partial\phi}{\partial z}$)

86.The vector differential operator ∇ is defined by _____

(Ans: $\nabla = i \frac{\partial}{\partial x} + j \frac{\partial}{\partial y} + k \frac{\partial}{\partial z}$)

87.The divergence of f is defined by _____

(Ans: $\nabla \cdot f = \frac{\partial f_1}{\partial x} + \frac{\partial f_2}{\partial y} + \frac{\partial f_3}{\partial z}$)

88.If f is a vector such that div $f=0$ then it is said to be _____

(Ans : Solenoidal)

89.If r is a vector of constant direction, then $r \times \frac{dr}{dt} =$ _____

a)0 b)1 c)2 d)-1

(Ans : a)

90.Say true or false

$\text{Grad}(\phi\Psi) = \phi \text{grad}\Psi + \Psi \text{grad}\phi$

(Ans : True)

91. If $r = xi + yj + zk$ then $\text{div } r =$ _____
a) 0 b) 3 c) 2 d) 1

(Ans : b)

92. Say true or false
 $\text{div}(u \times v) = v \cdot \text{curl } u + u \cdot \text{curl } v$

(Ans : False)

93. $\nabla^2 = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2}$ is called the _____

(Ans: Laplacian Operator)

94. If A & B are irrotational then $A \times B$ is _____

(Ans : Solenoidal)

95. Find $\nabla\phi$ to the surface $x^2y - 2xz^2 = 8$ at the point (1,0,2) is _____
a) $8i + j + 8k$ b) $4i + j + 8k$ c) $4i + 4j + 8k$ d) none

(Ans: a)

96. Say true or false
 $\text{div } f$ is a scalar

(Ans : True)

97. Say true or false
 $\text{curl } f$ is a vector

(Ans : True)

98. The value of $\nabla \times (\nabla\phi)$ is _____

(Ans : 0)

99. $\nabla\phi \cdot dr =$ _____
a) 1 b) 0 c) 2 d) -1

(Ans : b)

100. Say true or false
If $r = xi + yj + zk$ then $\text{curl } r = 0$

(Ans : True)

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(NATIONALLY RE-ACCREDITED WITH "A" GRADE BY NAAC)

PALANI.

STATISTICS

PART - A

1. ----- tell us the direction and extent of asymmetry in a series permit us to compare two or more series Ans: Measures of skewness
2. Karl pearson coefficient of skewness is defined by $S_{kp} = \frac{\text{Mean-Mode}}{\text{Standard deviation}}$ or $3(\text{Mean-Median})/\sigma$
Ans : (Mean-Mode)/(Standard deviation) or 3(Mean-Median)/ σ
3. Bowley's coefficient of Skewness is given by $S_{KB} = \frac{Q_3 + Q_1 - 2\text{Median}}{Q_3 - Q_1}$
Ans: $(Q_3 + Q_1 - 2\text{Median}) / (Q_3 - Q_1)$
4. The moment about mean are called the ----- Ans: Central moment(μ)
5. If $\beta_1 = 0$ the distribution is -----Ans: Symmetric
6. $\beta_1 > 0$ the frequency distribution has -----Ans: Positive Skewness
7. If $\beta_1 < 0$ the If frequency distribution has -----Ans: Negative Skewness
8. The r^{th} moment about any point A denoted by μ_r is defined by-----
Ans: $\mu_r = \sum f_i (X-A)^r / N$
9. The r^{th} moment about arithmetic mean X of a frequency distribution is given by -----Ans: $\mu_r = \sum f_i (X_i - X)^r / N$
10. $\beta_1 = \frac{\mu_3^2}{\mu_2^3}$ is called the measure of skewness Ans: $\beta_1 = \mu_3^2 / \mu_2^3$
11. In Symmetric distribution odd moments are always -----Ans: Zero
12. ----- is the degree of peakedness of a distribution usually taken relative to a normal distribution Ans: Kurtosis

13. For a curve the normal curve $\beta_2 < 3$ or $\gamma_2 < 0$ and such a curve is known as-----
-----Ans: Platykurtic

14. For a curve the normal curve $\beta_2 > 3$ or $\gamma_2 > 0$ and such a curve is known as-----
-----Ans: Leptokurtic

15. For a normal curve $\beta_2 = 3$ or $\gamma_2 = 0$ and such a curve is known as-----
Ans: Messokurtic

16. Karl Pearson and Bowley's are -----Ans: absolute measures of skewness

17. The most important measure of Kurtosis is the value of the coefficient β_2 is defined as-----
Ans: $\beta_2 = \mu_4 / \mu_2^2$

18. γ_2 is used as measure of defined as -----Ans: $\gamma_2 = \beta_2 - 3$

19. $\mu_2 = \mu_2^1 - (\mu_1^1)^2$ is the -----of the frequency distribution Ans: Variance

20. The first moment μ_1 about origin coincides with the -----of the frequency distribution. Ans: Arithmetic mean

21. The Karl Pearson co-efficient of correlation is _____

$$\text{Ans : } r = \frac{\sum(X_i - \bar{X})(Y_i - \bar{Y})}{N\sigma_x\sigma_y}$$

22. σ_x is the _____ of series X. Ans: standard deviation

23. The value of the co-efficient of correlation always lie between _____

A) +1 B) -1 C) ± 1 D) 0 Ans : ± 1

24. In correlation when $r = -1$, it means there is _____ negative correlation between the variables. Ans : Perfect

25. In correlation when $r = +1$, it means there is perfect _____ correlation between the variables. Ans : Positive

26. In correlation when _____, it means there is no relationship between the two variables. Ans : $r = 0$

27. The covariance of two series X and Y is defined by

$$\text{Ans : } \text{cov}(X, Y) = \frac{\sum(X_i - \bar{X})(Y_i - \bar{Y})}{N}$$

28. Direct method of finding out correlation co-efficient is

$$29. r = \frac{N\sum X_i Y_i - (\sum X_i)(\sum Y_i)}{\sqrt{N\sum X_i^2 - (\sum X_i)^2} \sqrt{N\sum Y_i^2 - (\sum Y_i)^2}}$$

30. The formula for calculating the co-efficient of correlation of grouped data is

$$\text{Ans : } r = \frac{N\sum fd_x d_y - (\sum fd_x)(\sum fd_y)}{\sqrt{N(\sum fd_x^2) - (\sum fd_x)^2} \sqrt{N(\sum fd_y^2) - (\sum fd_y)^2}}$$

21. when the numbers is large, the data are often classified into _____ called a correlation table. Ans : two way frequency distribution
22. The spearman's rank correlation co-efficient is defined as
 Ans : $R = 1 - \frac{6\sum D^2}{N(N^2-1)}$
23. The correlation co-efficient is independent of the change of _____
 Ans: origin and scale
24. If the variables x & y are uncorrelated then _____
 Ans: $\sum (X - \bar{X})(Y - \bar{Y}) = 0$
25. The _____ is added for each repeated rank of the variables.
 Ans: correction factor
26. The equation of the regression line of Y on X is _____ Ans: $Y - \bar{Y} = r \frac{\sigma_y}{\sigma_x} (X - \bar{X})$
27. The equation of the regression line of X on Y is _____ Ans : $X - \bar{X} = r \frac{\sigma_x}{\sigma_y} (Y - \bar{Y})$
28. If the curve is a straight line it is called a _____ between the two variables. Ans : line of regression
29. If there is a functional relationship between the two variables X_i & Y_i the points in the scatter diagram will cluster around some curve called the _____ Ans : curve of regression.
30. The regression co-efficient of X on Y is given by $b_{xy} = r \frac{\sigma_x}{\sigma_y}$
31. The regression co-efficient of Y on X is given by $b_{yx} = r \frac{\sigma_y}{\sigma_x}$
32. If one of the regression co-efficients is greater than unity the other is _____ Ans : less than unity.
33. The sign of the correlation co-efficient is the same as that of _____
 Ans : regression co-efficients.
34. The correlation co-efficient is the _____ between the regression co-efficients. Ans : geometric mean.
35. _____ of the regression co-efficients is greater than or equal to the correlation co-efficient. Ans: Arithmetic mean
36. The two variables are uncorrelated then the lines of regression are

- _____ to each other. Ans: perpendicular
47. The obtuse angle between the regression lines is given by
 Ans : $\tan^{-1}[(r^2-1/r) (\sigma_x\sigma_y/\sigma_x^2 + \sigma_y^2)]$.
48. The angle between two regression lines is given by
 Ans : $\theta = \tan^{-1}[(r^2-1/r) (\sigma_x\sigma_y/\sigma_x^2 + \sigma_y^2)]$.
- 34.45. If there is a perfect correlation between the two variables then the two regression lines _____ Ans : coincide.
50. If $r = \pm 1$, then $\theta = 0$ or π , then the two lines of regression are _____
 Ans : Parallel.
51. The probability attached to such an event is called the _____ and is denoted by $P(A/B)$. Ans: conditional probability
52. The two events A and B are dependent then the conditional probability of B given A is _____ Ans : $P(B/A) = P(AB)/P(A)$.
53. $P(A \cap B) = P(A) P(B/A)$ this relation is called _____ theorem for probabilities. Ans : multiplication
54. A is said to be independent of B if _____ Ans : $P(A/B) = P(A)$.
55. If A and B are two independent events then _____
 Ans : $P(A \cap B) = P(A)P(B)$.
56. _____ is known as Baye's rule. Ans : $P(A_i/B) = \{P(A_i)P(B/A_i)\}/P(B)$
57. The events $A_1 A_2 \dots A_n$ are said to be _____ if $P(A_1 \cap A_2 \dots \cap A_n) = P(A_1)P(A_2) \dots P(A_n)$. Ans : mutually independent
58. A set of events $A_1 A_2 \dots A_n$ are said to be _____ if $P(A_i \cap A_j) = P(A_i)P(A_j)$ for all $i \neq j$. Ans : pairwise independent
59. If $A_i \cap A_j = \emptyset$ for all i, j with $i \neq j$ then the sequence of subsets is said to be _____ Ans : mutually disjoint.
60. If $\bigcup_{n=1}^{\infty} A_n = S$ then the sequence of events is said to be _____
 Ans : exhaustive.
61. The mathematical expectation of X, denoted by $E(X)$, $E(X)$ is defined by _____ Ans : $\sum P_i X_i$.
62. A variable whose value is determined by the outcome of a random experiment is called a _____ Ans : random variable.
63. If the random variable takes the integer values it is called a _____
 Ans : discrete random variable.
64. If the random variable takes all values, within a certain interval then the random variable is called a _____ Ans : continuous random variable.

65. If $\int_{-\infty}^{\infty} f(x)dx=1$ then $f(x)$ is called the _____ of continuous random variable of X . Ans : probability density function
66. The function $F:R \rightarrow R$ defined by $F(x)=P(X \leq x)$ where $-\infty < x < \infty$ is called a _____ of the random variable of X .
67. A random variable is also known as stochastic variable.
68. The binomial distribution is also known as Bernoulli distribution.
69. A discrete random variable of the P.d.f. of _____ if $r=0,1 \dots n$ is said to have binomial distribution. Ans : $p(r)=nc \cdot p^r q^{n-r}$
70. M.g.f of a binomial distribution about the origin is _____ Ans : $(q+pe^t)^n$.
71. M.g.f about the mean np of a binomial distribution is _____ Ans : $(qe^{-pt} + pe^{qt})^n$.
72. Characteristic function of binomial distribution is _____ Ans : $(q + pe^{it})^n$.
73. Using M.g.f about the mean of the binomial distribution we can find _____
 μ_2, μ_3, μ_4 . Ans : central moments
74. If $X_1 \sim B(n_1, P)$, $X_2 \sim B(n_2, P)$ are independent random variables then $X_1 + X_2$ is _____ Ans : $B(n_1+n_2, P)$.
75. Recurrence relation for $p(x)$ in binomial distribution is _____
Ans: $P(x+1) = \frac{n-x}{x+1} (p/q)P(x)$.
76. Recurrence formula of moments of the binomial distribution is _____
Ans : $\mu_{r+1} = pq[nr\mu_{r-1} + d\mu_r]$
 dp .
77. If $(n+1)p$ is an integer will represent mode and the distribution is _____
Ans: bimodal.
78. If $(n+1)p$ is not an integer will represent mode and the distribution is _____
Ans : unimodal.
79. The standard deviation of binomial distribution is _____ Ans: \sqrt{npq} .
80. The mean of binomial distribution is _____ Ans : np .
81. The two independent constants n and p in the distribution are known as the _____ of the distribution. Ans : parameters
82. Find the mode of a binomial distribution $B(7, 1/4)$ is _____ Ans : 1 & 2.
83. The measure of skewness of the binomial distribution is _____ Ans : $\gamma_1 = \sqrt{\beta_1}$.
84. The measure of kurtosis of the binomial distribution is _____ Ans : $\gamma_2 = \beta_2 - 3$.
85. A is defined as $P(x) = P(X=x) = \begin{cases} \frac{e^{-\lambda} \lambda^x}{x!} & \text{if } x=0,1,2,\dots \\ 0 & \text{otherwise} \end{cases}$

- Where λ is a parameter of the distribution. Ans : poisson distribution
86. Mean of the poisson distribution is _____ Ans : λ .
87. The S.D of the poisson distribution is _____ Ans : $\sqrt{\lambda}$.
88. Recurrence relation of pdf in poisson distribution is _____
 Ans : $p(x+1) = (\lambda/x+1) p(x)$.
89. _____ of the poisson distribution is $\lambda-1 \leq x \leq \lambda$. Ans : Mode
90. If λ is an integer $\lambda-1$ is also an integer then mode is _____ of the poisson distribution. Ans: bimodal
91. If λ is not an integer ,then the mode will be represented _____ of poisson distribution. Ans : unimodal
92. M.g.f of the poisson distribution about $r=0$ is _____ Ans : $e^{\lambda(e^t-1)}$.
93. The value of $\lambda \sigma \gamma_1 \gamma_2 =$ _____ Ans : 1.
94. Characteristic function of the poisson distribution is _____ Ans: $e^{\lambda(e^{it}-1)}$.

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